

High-Resolution NMR Spectroscopy of Quadrupolar Nuclei in Solids: Satellite-Transition MAS with Self-Compensation for Magic-Angle Misset

Sharon E. Ashbrook and Stephen Wimperis*

School of Chemistry, University of Exeter, Exeter EX4 4QD, United Kingdom

Received March 14, 2002

Several methods are available for obtaining high-resolution NMR spectra of half-integer spin quadrupolar nuclei, such as ^{11}B , ^{23}Na ($I = 3/2$) and ^{17}O , ^{27}Al ($I = 5/2$), in powdered solids.^{1–3} Satellite-transition magic-angle spinning (STMAS)³ uses only conventional magic-angle spinning (MAS) hardware and, it has been claimed,⁴ improves significantly upon the signal-to-noise ratio obtained with the widely adopted multiple-quantum MAS (MQMAS) experiment.² The STMAS technique, however, requires that the sample rotation axis be set to the magic angle ($\cos^{-1}(1/\sqrt{3}) = 54.736^\circ$) with respect to the magnetic field B_0 with an accuracy of better than $\pm 0.004^\circ$,^{3,4} and this stringent requirement has severely limited the use of the method. Here, we propose a novel version of STMAS that self-compensates for magic-angle missets of up to $\pm 1.0^\circ$ and yet retains a sensitivity similar to that of MQMAS.

Under MAS, central transition ($m_1 = -1/2 \leftrightarrow m_1 = +1/2$) NMR spectra of half-integer spin quadrupolar nuclei remain broadened by a second-order quadrupolar interaction.⁵ In a reference frame rotating at the Larmor frequency ν_0 , the frequency of an observable $m_1 = \pm(q-1) \leftrightarrow m_1 = \pm q$ transition (with $q = 1/2, 3/2, \dots, I$) can be written for a rapidly spinning sample as the sum of two terms arising from the first- and second-order quadrupolar interactions, respectively:

$$\nu_{\pm(q-1) \leftrightarrow \pm q}^{(1)} = \pm(2q-1)\nu_Q^{\text{PAS}} d_{0,0}^2(\chi) d_{0,0}^2(\beta) \quad (1a)$$

$$\nu_{\pm(q-1) \leftrightarrow \pm q}^{(2)} = \frac{(\nu_Q^{\text{PAS}})^2}{\nu_0} \{A^0(I, q) + A^2(I, q) d_{0,0}^2(\chi) d_{0,0}^2(\beta) + A^4(I, q) d_{0,0}^4(\chi) d_{0,0}^4(\beta)\} \quad (1b)$$

Here, χ is the angle between the spinning axis and B_0 , β is the orientation of the quadrupole tensor (for simplicity, axial symmetry is assumed) with respect to the spinning axis, the coefficients $A^l(I, q)$ are derived from perturbation theory,^{2,3,6} and the quadrupole parameter, ν_Q^{PAS} , is given by $3e^2qQ\{4I(2I-1)h\}$. Spinning at the magic angle, the rank $l = 2$ rotation matrix element, $d_{0,0}^2(\chi = 54.736^\circ)$, is zero, and the first-order quadrupolar splitting is removed from all transitions in which it occurs. However, the anisotropic second-order shift survives because the $l = 4$ element, $d_{0,0}^4(\chi = 54.736^\circ)$, is nonzero. In a powder, there is a spherical distribution of β angles, and the result is a MAS spectrum with a central transition (CT) that has a rank $l = 4$ broadening proportional to $A^4(I, 1/2)(\nu_Q^{\text{PAS}})^2/\nu_0$ and an isotropic quadrupolar shift equal to $A^0(I, 1/2)(\nu_Q^{\text{PAS}})^2/\nu_0$.

The pulse sequence for a shifted-echo⁷ two-dimensional STMAS experiment⁴ is shown in Figure 1a. This technique removes the first- and second-order quadrupolar broadening (i) by using MAS to suppress the first-order splitting and the rank $l = 2$ component of the second-order interaction and (ii) by correlating the two $q =$

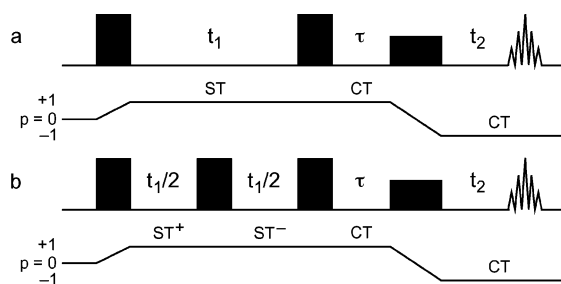


Figure 1. Pulse sequences and coherence pathways for (a) STMAS and (b) STMAS with self-compensation for magic-angle misset (SCAM). In (b), a 100-step phase cycle was used: first pulse, 0° ; second pulse, $0^\circ, 72^\circ, 144^\circ, 216^\circ, 288^\circ$; third pulse, $5(0^\circ), 5(72^\circ), 5(144^\circ), 5(216^\circ), 5(288^\circ)$; fourth pulse, $25(0^\circ), 25(90^\circ), 25(180^\circ), 25(270^\circ)$; receiver, $25(0^\circ), 25(180^\circ)$.

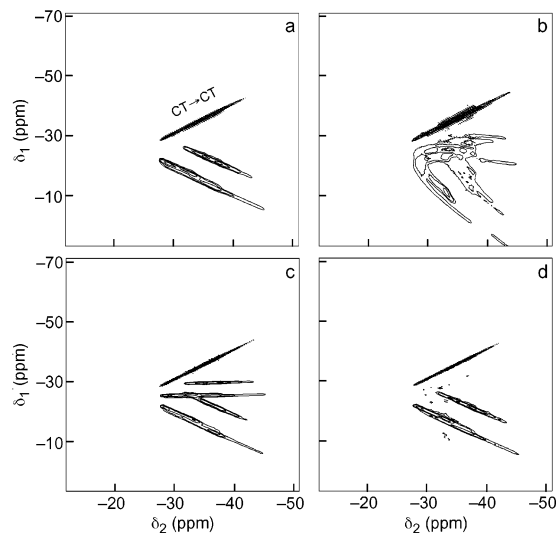


Figure 2. ^{87}Rb ($\nu_0 = 130.9$ MHz) NMR spectra of RbNO_3 . (a) STMAS spectrum at the magic angle. The three pulse durations were $1.7 \mu\text{s}$, $1.5 \mu\text{s}$ ($\nu_1 = |\gamma B_1| \approx 150$ kHz), and, for the final reduced-power pulse, $30 \mu\text{s}$. (b) STMAS spectrum with the spinning angle misset by $\sim 0.07^\circ$. (c) SCAM-STMAS spectrum at the magic angle. (d) SCAM-STMAS spectrum with the spinning angle misset by $\sim 0.07^\circ$. The additional pulse durations of (c) $1.0 \mu\text{s}$ and (d) $2.0 \mu\text{s}$ were found by experimental optimization. The MAS rate, ν_R , was 20 kHz.

$3/2$ satellite transitions (usually, although $q = 5/2, 7/2$, and $9/2$ transitions have also been used⁴) in the t_1 period with the $q = 1/2$ central transition in the t_2 period such that an echo forms when $t_2/t_1 = A^4(I, 3/2)/A^4(I, 1/2)$, refocusing the $l = 4$ second-order broadening. As desired, the method retains resolution due to isotropic (rank $l = 0$) shifts. Figure 2a shows the ^{87}Rb ($I = 3/2$) STMAS spectrum of RbNO_3 . The three crystallographically inequivalent Rb sites appear as three “ridge” line shapes (two lie very close together) with gradients equal to $A^4(3/2, 3/2)/A^4(3/2, 1/2) = -8/9$. In addition to these desired ST \rightarrow CT ridges, an uninformative “diagonal” peak also appears along a gradient of $+1$

* To whom correspondence should be addressed. Fax: +44-1392-263434. E-mail: s.wimperis@exeter.ac.uk.

due to CT \rightarrow CT coherence transfer. A high-resolution or “isotropic” spectrum can be obtained by projecting the two-dimensional spectrum onto an axis orthogonal to the $A^4(3/2, 3/2)/A^4(3/2, 1/2)$ gradient, as shown in Figure 3a.

The STMAS experiment requires that the spinning angle χ be set to the magic angle with high accuracy.^{3,4} If χ deviates from this, then the first-order quadrupolar splitting is reintroduced. For example, the two $q = 3/2$ satellites, $m_1 = \pm 1/2 \leftrightarrow m_1 = \pm 3/2$, are split by $4\nu_Q^{\text{PAS}} d_{0,0}^2(\chi) d_{0,0}^2(\beta)$, and, because a typical value of ν_Q^{PAS} is perhaps 250 kHz, the angle χ must not deviate from 54.736° by more than about $\pm 0.004^\circ$ if the splitting is not to exceed 100 Hz. In contrast, the second-order quadrupolar shifts of the central and satellite transitions are unaffected by a small deviation of χ from the magic angle. For example, if $\nu_Q^{\text{PAS}} = 250$ kHz and $\nu_0 = 100$ MHz, then $(\nu_Q^{\text{PAS}})^2/\nu_0$ is only 625 Hz, and even a $\pm 1.0^\circ$ deviation of χ changes the second-order shifts by only a few tens of Hz. Figure 2b shows the ^{87}Rb STMAS spectrum of RbNO_3 recorded with the angle χ miset by an amount estimated to be 0.07° . A first-order splitting has been reintroduced into the satellite-transition dimension (δ_1), and the resolution has been spoiled.

The pulse sequence for a version of STMAS that is self-compensated for angle miset (SCAM) is shown in Figure 1b. As in Figure 1a, this is a shifted-echo experiment and yields absorptive line shapes. The novel feature of the new experiment is a pulse in the middle of the t_1 period that transfers coherence between the two $q = 3/2$ satellite transitions. The $m_1 = +1/2 \leftrightarrow m_1 = +3/2$ and $m_1 = -1/2 \leftrightarrow m_1 = -3/2$ transitions (ST^+ and ST^-) have first-order quadrupolar frequencies that are equal in magnitude but opposite in sign (see eq 1a); hence, by inducing $\text{ST}^\pm \rightarrow \text{ST}^\mp$ transfer, the unwanted first-order splitting is refocused. Crucially, the new pulse is phase-cycled so as to maintain the sign of the coherence order, p , and avoid premature refocusing of the second-order shift.

Figure 2c shows the ^{87}Rb SCAM-STMAS spectrum of RbNO_3 recorded with the spinning angle χ set accurately to the magic angle as in Figure 2a. The spectrum is similar to that in Figure 2a, except that additional ridges appear midway between the CT \rightarrow CT \rightarrow CT diagonal peak and the desired $\text{ST}^\pm \rightarrow \text{ST}^\mp \rightarrow$ CT and $\text{ST}^\pm \rightarrow \text{ST}^\pm \rightarrow$ CT ridges due to unwanted CT $\rightarrow \text{ST}^\pm \rightarrow$ CT and $\text{ST}^\pm \rightarrow \text{CT} \rightarrow$ CT transfer. Figure 2d shows the ^{87}Rb SCAM-STMAS spectrum when χ is miset by $\sim 0.07^\circ$ as in Figure 2b. The unwanted CT $\rightarrow \text{ST}^\pm \rightarrow$ CT and $\text{ST}^\pm \rightarrow \text{CT} \rightarrow$ CT ridges are now split by the residual first-order quadrupolar interaction in δ_1 and are barely visible at the contour levels used. Similarly, the $\text{ST}^\pm \rightarrow \text{ST}^\pm \rightarrow$ CT components of the desired ridges are now split and not visible. However, three narrow ridge line shapes with gradients of $\sim 8/9$ remain prominent, arising from $\text{ST}^\pm \rightarrow \text{ST}^\mp \rightarrow$ CT pathways that refocus the first-order splitting.

The isotropic projection of a ^{87}Rb SCAM-STMAS spectrum, shown in Figure 3b, clearly reveals the three Rb sites in RbNO_3 but also shows reduced sensitivity as compared with STMAS performed with χ set accurately (Figure 3a). However, the sensitivity is approximately the same as that in the isotropic ^{87}Rb MQMAS projection (also performed with χ miset by $\sim 0.07^\circ$) shown in Figure 3c. Results broadly similar to these have also been obtained on RbNO_3 at a lower MAS rate (10 kHz) and on Rb_2SO_4 and, using ^{27}Al ($I = 5/2$) NMR, on $\text{Al}(\text{acac})_3$ and andalusite, Al_2SiO_5 .

Figure 4a shows the ^{27}Al “split- t_1 ”⁴ STMAS ($q = 3/2$) spectrum of kyanite, Al_2SiO_5 , recorded with the spinning angle χ set as accurately as possible using our normal procedure.⁴ There are four Al sites in kyanite, two of which have large ν_Q^{PAS} values of about 750 kHz. These two long ridge line shapes at $\delta_1 \approx 25$ ppm are not resolved in this spectrum, however, and have a distinctive “hairpin” appearance arising from residual first-order (or, possibly, third-

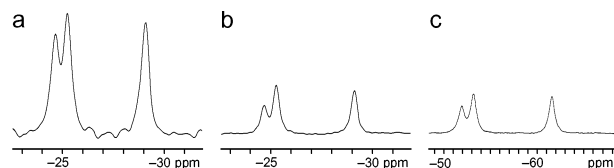


Figure 3. Absolute-intensity ^{87}Rb isotropic projections of (a) on-angle STMAS, (b) off-angle SCAM-STMAS, and (c) off-angle MQMAS (split- t_1 shifted-echo, $\nu_1 \approx 150$ kHz, $\nu_R = 20$ kHz) NMR spectra of RbNO_3 . In (b), an experimentally optimized composite pulse, $(1.8 \mu\text{s})_x(1.75 \mu\text{s})_{-x}$, was used in place of the simple SCAM pulse to enhance the sensitivity by $\sim 20\%$. In (c), an experimentally optimized fast-amplitude-modulation (FAM) conversion pulse,⁸ $\{(0.8 \mu\text{s})_x - \tau - (0.8 \mu\text{s})_{-x} - \tau - \}_3$ with $\tau = 0.8 \mu\text{s}$, was used to enhance the MQMAS sensitivity by $\sim 80\%$. Each experiment was performed in 120 min with a maximum t_1 period of 24 ms.

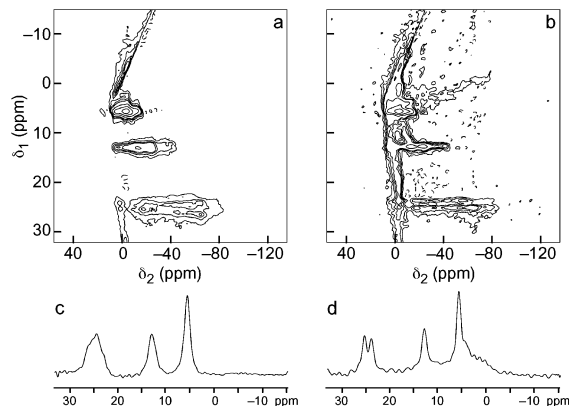


Figure 4. ^{27}Al ($\nu_0 = 104.3$ MHz) NMR spectra of Al_2SiO_5 ($\nu_1 \approx 100$ kHz, $\nu_R = 30$ kHz). (a) Split- t_1 STMAS ($q = 3/2$) spectrum with the spinning angle set as accurately as possible using our normal procedure. (b) Split- t_1 SCAM-STMAS ($q = 3/2$) spectrum with the angle miset by $\sim 0.09^\circ$. (c) and (d) Normalized-intensity isotropic projections of (a) and (b).

order) splittings in δ_1 (χ would need to be miset by less than $\pm 0.001^\circ$ for the first-order splitting to be less than 100 Hz). In contrast, all four ridge line shapes are resolved in the split- t_1 SCAM-STMAS spectrum in Figure 4b, recorded with χ miset by $\sim 0.09^\circ$; the two long ridges are now very narrow in δ_1 and precisely parallel to δ_2 . This increased resolution is confirmed in the isotropic projections in Figure 4c and d.

In summary, the SCAM-STMAS NMR experiment yields superior isotropic resolution without accurate adjustment of the spinning angle (indeed, χ must be miset if the unwanted ridges in Figure 2c are to be avoided) and appears to have a sensitivity that is comparable with MQMAS. Many SCAM experiments similar to that in Figure 1b can be devised, including ones that utilize multiple-quantum satellite transitions.

Acknowledgment. We thank Professor M. H. Levitt (Southampton, U.K.) for suggesting this line of investigation to us and EPSRC for support (grant GR/N07622).

References

- (1) (a) Samoson, A.; Lippmaa, E.; Pines, A. *Mol. Phys.* **1988**, *65*, 1013. (b) Llor, A.; Viret, J. *Chem. Phys. Lett.* **1988**, *152*, 248.
- (2) Frydman, L.; Harwood, J. S. *J. Am. Chem. Soc.* **1995**, *117*, 5367.
- (3) (a) Gan, Z. *J. Am. Chem. Soc.* **2000**, *122*, 3242. (b) Gan, Z. *J. Chem. Phys.* **2001**, *114*, 10845.
- (4) (a) Pike, K. J.; Ashbrook, S. E.; Wimperis, S. *Chem. Phys. Lett.* **2001**, *345*, 400. (b) Ashbrook, S. E.; Wimperis, S. *J. Magn. Reson.* **2002**, *156*, 269.
- (5) Ganapathy, S.; Schramm, S.; Oldfield, E. J. *Chem. Phys.* **1982**, *77*, 4360.
- (6) Amoureux, J. P. *Solid State Nucl. Magn. Reson.* **1993**, *2*, 83.
- (7) Grandinetti, P. J.; Baltisberger, J. H.; Llor, A.; Lee, Y. K.; Werner, U.; Eastman, M. A.; Pines, A. *J. Magn. Reson., Ser. A* **1993**, *103*, 72.
- (8) Madhu, P. K.; Goldburd, A.; Frydman, L.; Vega, S. *Chem. Phys. Lett.* **1999**, *307*, 41.

JA0203869